

# Leptonic CP Phase Measurement & New Physics

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Jarah Evslin, **SFG**, Kaoru Hagiwara, JHEP **1602** (2016) 137 [arXiv:1506.05023]  
**SFG**, Pedro Pasquini, M. Tortola, J. W. F. Valle, PRD **95** (2017) No.3, 033005 [arXiv:1605.01670]  
**SFG**, Alexei Smirnov, JHEP **1610** (2016) 138 [arXiv:1607.08513]  
**SFG** [arXiv:1704.08518]  
**SFG**, Stephen Parke [arXiv:1812.08376]

Georg G. Raffelt

# Stars as Laboratories for Fundamental Physics

The Astrophysics of Neutrinos, Axions, and Other  
Weakly Interacting Particles

In the standard model, neutrinos have been assigned the most minimal properties compatible with experimental data: zero mass, zero charge, zero dipole moments, zero decay rate, zero almost everything.

**Neutrinos are not just invisible but very boring!**

# Lazy Neutrino



**Nothing can interest me!!!**

# Why neutrino mass & oscillation?

- **Higgs boson**  $\Rightarrow$  electroweak symmetry breaking & mass.
- **Chiral symmetry breaking**  $\Rightarrow$  majority of mass.
- **The world seems not affected by the tiny neutrino mass?**
  - Neutrino mass  $\Rightarrow$  Mixing
  - 3 Neutrino  $\Rightarrow$  possible **CP violation**
  - CP violation  $\Rightarrow$  **Leptogenesis**
  - **Leptogenesis**  $\Rightarrow$  **Matter-Antimatter Asymmetry**
  - There is something left in the Universe.
  - Baryogenesis from quark mixing is not enough.
- Majorana  $\nu \Leftrightarrow$  **Lepton Number Violation**
- **Residual  $\mathbb{Z}_2$  Symmetries:**  $\cos \delta_D = \frac{(s_s^2 - c_s^2 s_r^2)(c_a^2 - s_a^2)}{4c_a s_a c_s s_s s_r}$

1108.0964

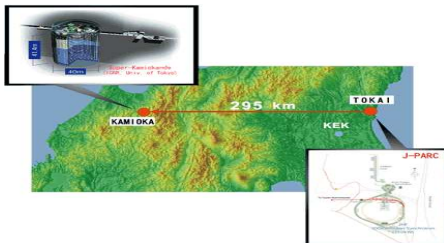
1104.0602

## $\nu$ Oscillation Data

(for NH)	$-1\sigma$	Best Value	$+1\sigma$
$\Delta m_s^2 \equiv \Delta m_{12}^2$ ( $10^{-5}\text{eV}^2$ )	7.37	<b>7.56</b>	7.75
$ \Delta m_a^2 \equiv \Delta m_{13}^2 $ ( $10^{-3}\text{eV}^2$ )	2.51	<b>2.55</b>	2.59
$\sin^2 \theta_s$ ( $\theta_s \equiv \theta_{12}$ )	0.305 ( $33.5^\circ$ )	0.321 ( <b><math>34.5^\circ</math></b> )	0.339 ( $35.6^\circ$ )
$\sin^2 \theta_a$ ( $\theta_a \equiv \theta_{23}$ )	0.412 ( $39.9^\circ$ )	0.430 ( <b><math>41.0^\circ</math></b> )	0.450 ( $42.1^\circ$ )
$\sin^2 \theta_r$ ( $\theta_r \equiv \theta_{13}$ )	0.02080 ( $8.29^\circ$ )	0.02155 ( <b><math>8.44^\circ</math></b> )	0.02245 ( $8.62^\circ$ )
$\delta_D, \delta_{Mi}$	?, ??	?, ??	?, ??

# CP Measurement @ Accelerator Exps

- T2K



- $\text{NO}\nu\text{A}$



- DUNE/T2KII/T2HK/T2HKK/T2KO; MOMENT/ADS-CI/DAE $\delta$ ALUS; Super-PINGU

# The Dirac CP Phase $\delta_D$ @ Accelerator Exp

- To leading order in  $\alpha = \frac{\delta M_{21}^2}{|\delta M_{31}^2|} \sim 3\%$ , the oscillation probability relevant to measuring  $\delta_D$  @ T2(H)K,

$$P_{\nu_\mu \rightarrow \nu_e} \approx 4s_a^2 c_r^2 s_r^2 \sin^2 \phi_{31} - 8c_a s_a c_r^2 s_r c_s s_s \sin \phi_{21} \sin \phi_{31} [\cos \delta_D \cos \phi_{31} \pm \sin \delta_D \sin \phi_{31}]$$
$$P_{\bar{\nu}_\mu \rightarrow \bar{\nu}_e}$$

for  $\nu$  &  $\bar{\nu}$ , respectively.  $[\phi_{ij} \equiv \frac{\delta m_{ij}^2 L}{4E_\nu}]$

- $\nu_\mu \rightarrow \nu_\mu$  Exps measure  $\sin^2(2\theta_a)$  precisely, but not  $\sin^2 \theta_a$ .
- Run both  $\nu$  &  $\bar{\nu}$  modes @ first peak  $[\phi_{31} = \frac{\pi}{2}, \phi_{21} = \alpha \frac{\pi}{2}]$ ,

$$P_{\bar{\nu}_\mu \rightarrow \bar{\nu}_e} + P_{\nu_\mu \rightarrow \nu_e} = 2s_a^2 c_r^2 s_r^2,$$

$$P_{\bar{\nu}_\mu \rightarrow \bar{\nu}_e} - P_{\nu_\mu \rightarrow \nu_e} = \alpha \pi \sin(2\theta_s) \sin(2\theta_r) \sin(2\theta_a) \cos \theta_r \sin \delta_D.$$

# The Dirac CP Phase $\delta_D$ @ Accelerator Exp

Accelerator experiment, such as **T2(H)K**, uses off-axis beam to compare  $\nu_e$  &  $\bar{\nu}_e$  appearance @ the oscillation maximum.

- **Disadvantages:**

- **Efficiency:**

- Proton accelerators produce  $\nu$  more efficiently than  $\bar{\nu}$  ( $\sigma_\nu > \sigma_{\bar{\nu}}$ ).
- The  $\bar{\nu}$  mode needs more beam time [ **$T_{\bar{\nu}} : T_\nu = 2 : 1$** ].
- Undercut statistics  $\Rightarrow$  Difficult to reduce the uncertainty.

- **Degeneracy:**

- Only  **$\sin \delta_D$**  appears in  $P_{\nu_\mu \rightarrow \nu_e}$  &  $P_{\bar{\nu}_\mu \rightarrow \bar{\nu}_e}$ .
- Cannot distinguish  $\delta_D$  from  $\pi - \delta_D$ .

- **CP Uncertainty**  $\frac{\partial P_{\mu e}}{\partial \delta_D} \propto \cos \delta_D \Rightarrow \Delta(\delta_D) \propto$   **$1 / \cos \delta_D$** .

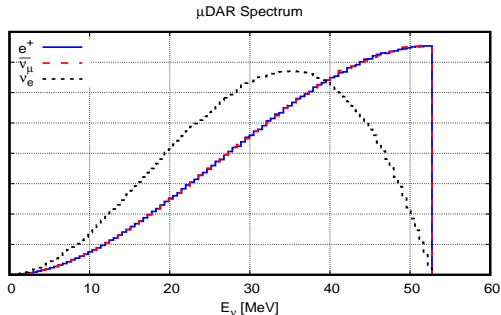
- **Solution:**

**Measure  $\bar{\nu}$  mode with  $\mu^+$  decay @ rest ( $\mu$ DAR)**



# $\mu$ DAR $\bar{\nu}$ Oscillation Experiments

- A cyclotron produces 800 MeV proton beam @ fixed target.
- Produce  $\pi^\pm$  which stops &
  - $\pi^-$  is absorbed,
  - $\pi^+$  decays @ rest:  $\pi^+ \rightarrow \mu^+ + \nu_\mu$ .
- $\mu^+$  stops & decays @ rest:  $\mu^+ \rightarrow e^+ + \bar{\nu}_\mu + \nu_e$ .

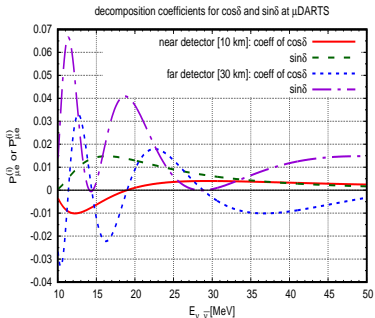
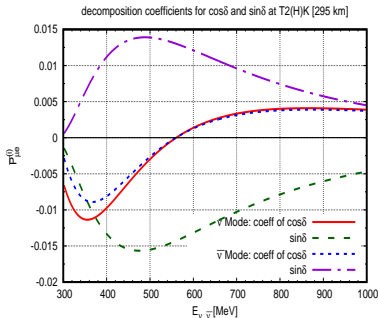


- $\bar{\nu}_\mu$  travel in all directions, oscillating as they go.
- A detector measures the  $\bar{\nu}_e$  from  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  **oscillation**.

# Accelerator + $\mu$ DAR Experiments

Combining  $\nu_\mu \rightarrow \nu_e$  @ accelerator [narrow peak @ 550 MeV] &  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  @  $\mu$ DAR [wide peak  $\sim$  45 MeV] solves the 2 problems:

- **Efficiency:**
  - $\bar{\nu}$  @ high intensity,  $\mu$ DAR is plentiful enough.
  - Accelerator Exps can devote all run time to the  $\nu$  mode. With same run time, the statistical uncertainty drops by  $\sqrt{3}$ .
- **Degeneracy:** (**decomposition in propagation basis** [1309.3176])



# DAE $\delta$ ALUS

- It's the **FIRST** proposal along this line:
  - **3**  $\mu$ DAR with **3** high-intensity cyclotron complexes.
  - **1** detector.
  - Different baselines: **1.5, 8 & 20** km to break degeneracies.
- **Disadvantages:**
  - The scattering lepton from IBD @ low energy is **isotropic**.
  - **Cannot** distinguish  $\bar{\nu}_e$  from different sources
  - Baseline **cannot be measured**.
  - Cyclotrons **cannot** run simultaneously (20~25% duty factor).
  - **Large** statistical uncertainty.
  - **Higher intensity** is necessary.
  - **Expensive** & Technically **challenging**.

# New Proposals

1  $\mu$ DAR source + 2 detectors

## Advantages

- Full (**100%**) duty factor!
- **Lower** intensity:  $\sim 9\text{mA}$  [ $\sim 4\times$  lower than DAE $\delta$ ALUS]
- Not far beyond the current state-of-art technology of cyclotron [2.2mA @ Paul Scherrer Institute]
- MUCH **cheaper** & technically **easier**.
  - Only one cyclotron.
  - Lower intensity.

## Disadvantage?

- A second detector!
  - $\mu$ DAR with Two Scintillators ( $\mu$ DARTS) [Ciuffoli, Evslin & Zhang, 1401.3977] also Smirnov, Hu, Li & Ling [1802.03677, 1808.03795]
  - Tokai 'N Toyama to(2) Kamioka (TNT2K) [Evslin, Ge & Hagiwara, 1506.05023]

# $\mu$ DARTS – JUNO & RENO50

- **Two detectors** are suggested to overcome the **unknown energy response**. [Ciuffoli et al., PRD 2014; 1307.7419]

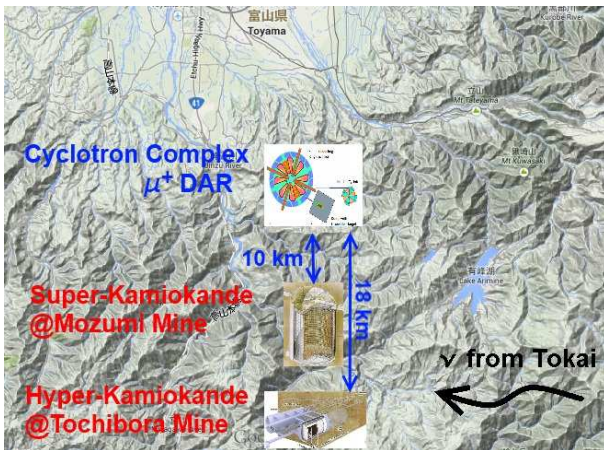


See also Smirnov, Hu, Li & Ling [1802.03677, 1808.03795]

- China Atomic Energy Center is proposing a cyclotron.

# TNT2K

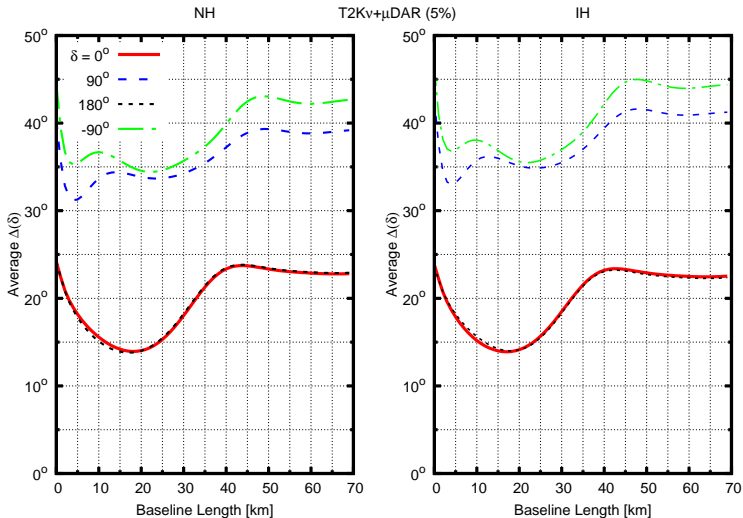
- T2(H)K +  $\mu$ SK +  $\mu$ HK



- $\mu$ DAR is also useful for **material**, **medicine** industries in Toyama

# $\delta_D$ Precision @ TNT2K

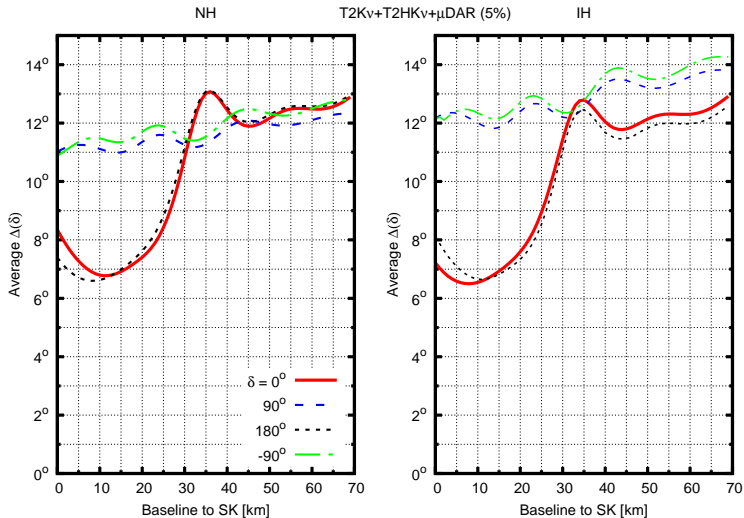
Evslin, Ge & Hagiwara [1506.05023]



Simulated by NuPro, <http://nupro.hepforge.org/>

# $\delta_D$ Precision @ TNT2K

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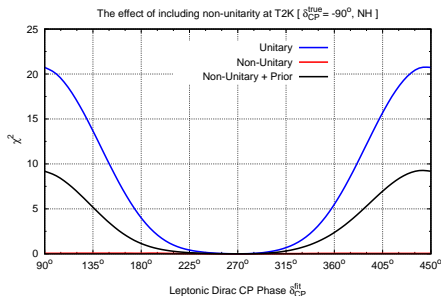


# Non-Unitarity Mixing (NUM)

Ge, Pasquini, Tortola & Valle [1605.01670]

$$N = N^{NP} U = \begin{pmatrix} \alpha_{11} & 0 & 0 \\ |\alpha_{21}| e^{i\phi} & \alpha_{22} & 0 \\ \alpha_{31} & \alpha_{32} & \alpha_{33} \end{pmatrix} U.$$

$$P_{\mu e}^{NP} = \alpha_{11}^2 \left\{ \alpha_{22}^2 \left[ c_a^2 |S'_{12}|^2 + s_a^2 |S'_{13}|^2 + 2c_a s_a (\cos \delta_D \mathbb{R} - \sin \delta_D \mathbb{I})(S'_{12} S'_{13}^*) \right] + |\alpha_{21}|^2 P_{ee} \right. \\ \left. + 2\alpha_{22} |\alpha_{21}| \left[ c_a (c_\phi \mathbb{R} - s_\phi \mathbb{I})(S'_{11} S'_{12}^*) + s_a (c_{\phi+\delta_D} \mathbb{R} - s_{\phi+\delta_D} \mathbb{I})(S'_{11} S'_{13}^*) \right] \right\}.$$



# NUM vs Seesaw Mechanism

- Heavy neutrinos

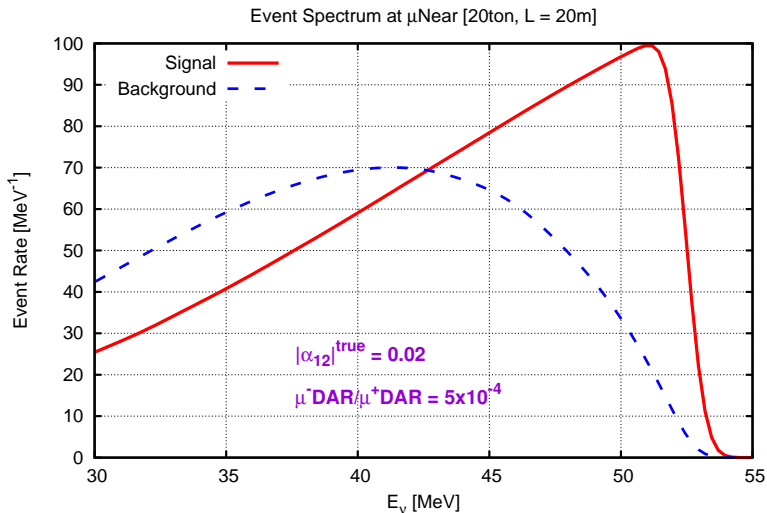
$$\bar{\nu} M_D \mathcal{N} + h.c. + \bar{\mathcal{N}} M_N \mathcal{N} = \begin{pmatrix} \bar{\nu} & \bar{\mathcal{N}} \end{pmatrix} \begin{pmatrix} 0 & M_D \\ M_D^T & M_N \end{pmatrix} \begin{pmatrix} \nu \\ \mathcal{N} \end{pmatrix}$$

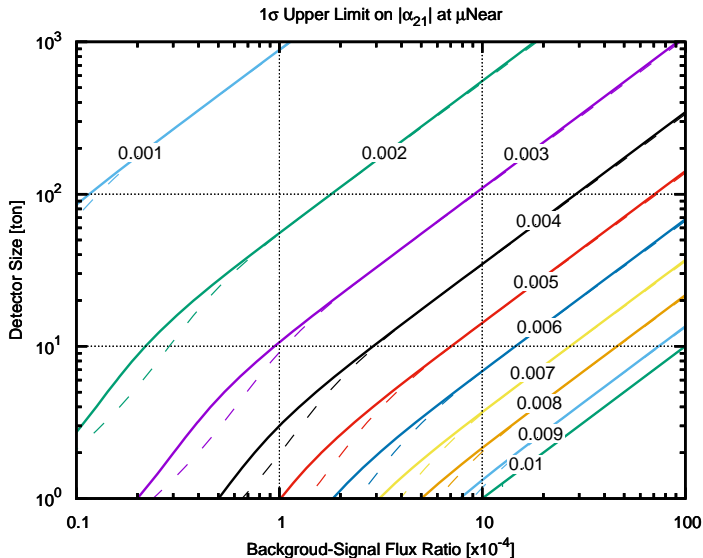
- Seesaw Mechanism

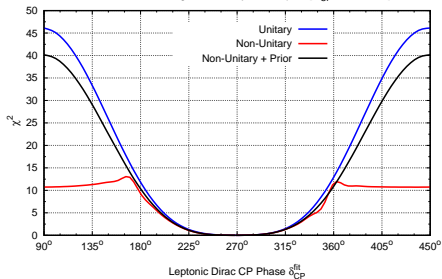
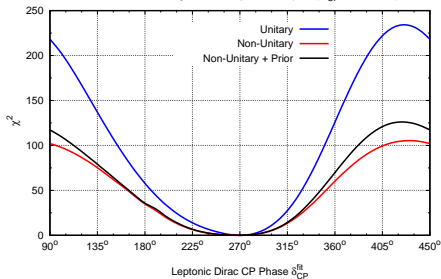
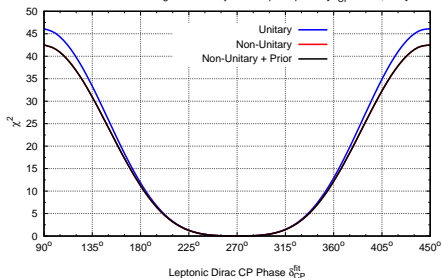
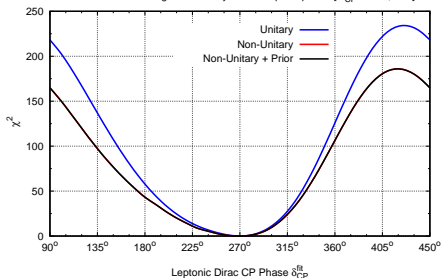
$$M_\nu = -M_D M_N^{-1} M_D^T, \quad \nu' = \nu + M_D M_N^{-1} \mathcal{N}$$



$$P_{\mu e}^{NP}(L \rightarrow 0) = \alpha_{11}^2 |\alpha_{21}|^2 P_{ee} \approx \alpha_{11}^2 |\alpha_{21}|^2 \approx |\alpha_{21}|^2$$





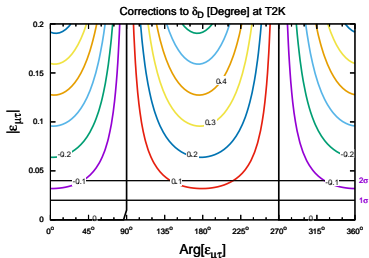
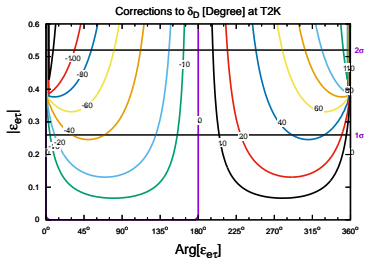
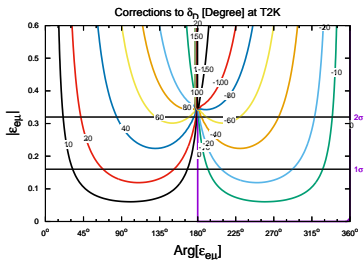
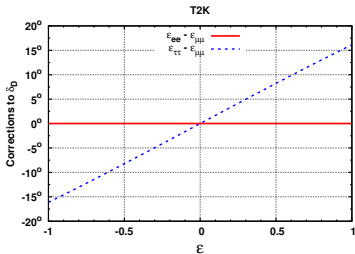
The effect of including non-unitarity at T2K+ $\mu$ SK [  $\delta_{CP}^{true} = -90^\circ$ , NH ]

 The effect of including non-unitarity at T2HK+ $\mu$ HK [  $\delta_{CP}^{true} = -90^\circ$ , NH ]

 The effect of including non-unitarity at T2K+ $\mu$ SK+ $\mu$ Near [  $\delta_{CP}^{true} = -90^\circ$ , NH ]

 The effect of including non-unitarity at T2HK+ $\mu$ HK+ $\mu$ Near [  $\delta_{CP}^{true} = -90^\circ$ , NH ]


$$\mathcal{H} \equiv \frac{1}{2\mathbf{E}_\nu} U \begin{pmatrix} 0 & & \\ & \Delta m_s^2 & \\ & & \Delta m_a^2 \end{pmatrix} U^\dagger + V_{cc} \begin{pmatrix} 1 + \epsilon_{ee} & \epsilon_{e\mu} & \epsilon_{e\tau} \\ \epsilon_{e\mu}^* & \epsilon_{\mu\mu} & \epsilon_{\mu\tau} \\ \epsilon_{e\tau}^* & \epsilon_{\mu\tau}^* & \epsilon_{\tau\tau} \end{pmatrix}$$

- Standard Interaction –  $V_{cc}$  (also  $V_{nc}$ )
- Non-Standard Interaction –  $\epsilon_{\alpha\beta}$ 
  - **Diagonal**  $\epsilon_{\alpha\alpha}$  are real
  - **Off-diagonal**  $\epsilon_{\alpha\neq\beta}$  are complex
  - **Both can fake CP**
- $Z'$  in LMA-Dark model with  $L_\mu - L_\tau$  gauged as  $U(1)$ 
  - $M_{Z'} \sim \mathcal{O}(10)\text{MeV}$
  - $g_{Z'} \sim 10^{-5}$

# Faked CP with NSI

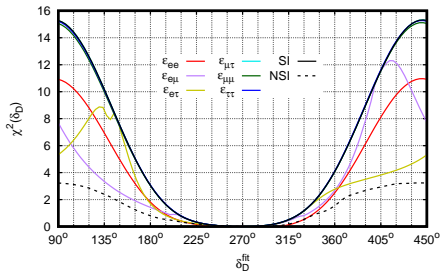
SFG & Alexei Smirnov [arXiv:1607.08513]



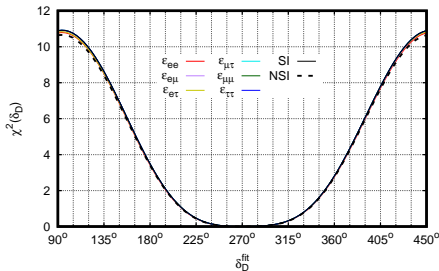
# CP Sensitivity at T2K & $\mu$ SK

SFG & Alexei Smirnov [arXiv:1607.08513]

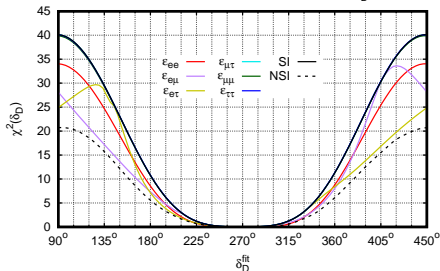
The effect of NSI on the CP sensitivity at T2K [  $\delta_D^{\text{true}} = -90^\circ$  ]



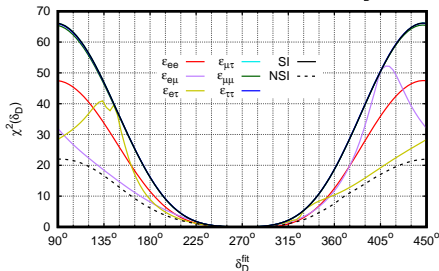
The effect of NSI on the CP sensitivity at  $\mu$ SK [  $\delta_D^{\text{true}} = -90^\circ$  ]



The effect of NSI on the CP sensitivity at T2K+ $\mu$ SK [  $\delta_D^{\text{true}} = -90^\circ$  ]



The effect of NSI on the CP sensitivity at  $\nu$ T2K+ $\mu$ SK [  $\delta_D^{\text{true}} = -90^\circ$  ]





- **Vector NSI**

$$\mathcal{L}_{\text{cc}}^{\text{eff}} = \frac{g_{\alpha\rho}g_{\beta\sigma}^*}{2} \frac{1}{-m_V^2} (\bar{\nu}_\alpha \gamma_\mu P_L \nu_\beta) (\bar{\ell}_\sigma \gamma^\mu P_L \ell_\rho) ,$$

which is **vector-vector type vertex**.

- **Scalar Mediator**

$$-\mathcal{L} = \frac{1}{2}m_\phi^2\phi^2 + \frac{1}{2}M_{\alpha\beta}\bar{\nu}_\alpha\nu_\beta + y_{\alpha\beta}\phi\bar{\nu}_\alpha\nu_\beta + Y_{\alpha\beta}\phi\bar{f}_\alpha f_\beta + h.c. ,$$

Due to **forward scattering**, the **effective Lagrangian** is

$$\mathcal{L}_{\text{eff}}^S \propto y_{\alpha\beta} Y_{ee} [\bar{\nu}_\alpha(p_3)\nu_\beta(p_2)] [\bar{e}(p_1)e(p_4)] ,$$

which is a **scalar-scalar type vertex**  $\Rightarrow$  **significant phenomenological consequences**.

# EOM & Effective Hamiltonian with Scalar NSI

- Two-Point Correlation Function

$$\delta\Gamma_S = \frac{y_{\alpha'\beta'} y_{ee}}{m_\phi^2} \langle \nu_\alpha | \bar{\nu}_{\alpha'} \nu_{\beta'} | \nu_\beta \rangle \langle e | \bar{e} e | e \rangle,$$

$$\delta\bar{\Gamma}_S = \frac{y_{\beta'\alpha'} y_{ee}}{m_\phi^2} \langle \bar{\nu}_\alpha | \bar{\nu}_{\alpha'} \nu_{\beta'} | \bar{\nu}_\beta \rangle \langle e | \bar{e} e | e \rangle.$$

- Equation of Motion

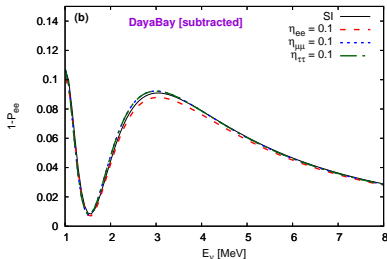
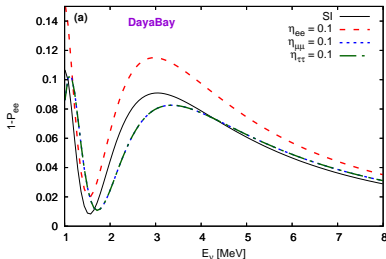
$$\bar{\nu}_\beta \left[ i\partial_\mu \gamma^\mu + \left( M_{\beta\alpha} + \frac{\mathbf{n}_e y_e \mathbf{Y}_{\alpha\beta}}{m_\phi^2} \right) \right] \nu_\alpha = 0,$$

- Effective Hamiltonian

$$\mathcal{H} \approx E_\nu + \frac{(M + \mathbf{M}_S)(M + \mathbf{M}_S)^\dagger}{2E_\nu} \pm V_{SI},$$

# Density Subtraction for Reactor Anti-Neutrinos

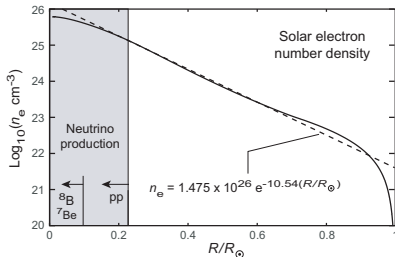
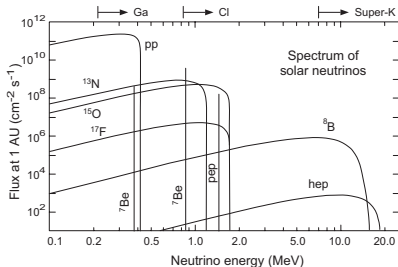
- Since the reactor anti-neutrino experiments (**Daya Bay & JUNO**) are the most precise ones, we do subtraction according to them:



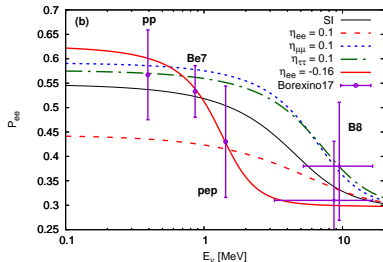
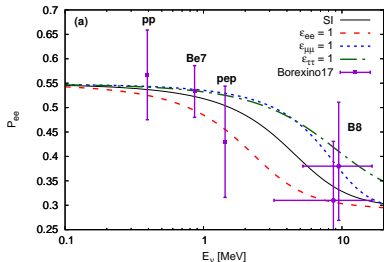
$$\tilde{M} \rightarrow \tilde{M} + \tilde{\mathbf{M}}_S \frac{\rho - \rho_S}{\rho_S}$$

- Then **no constraint** on **scalar NSI** from reactor experiments!

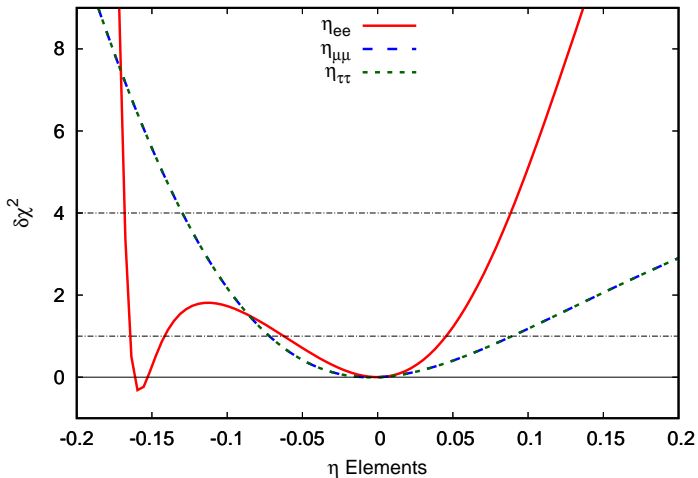
# Solar Neutrino



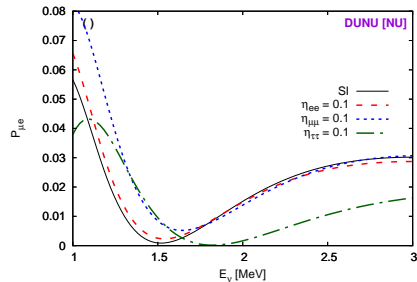
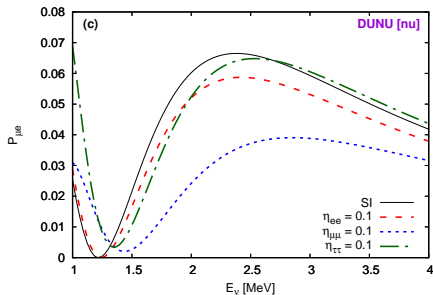
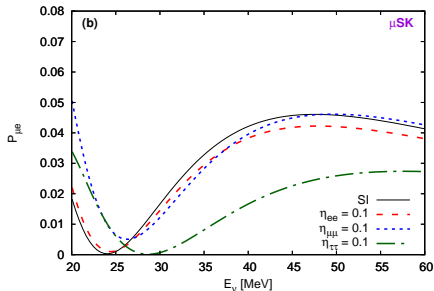
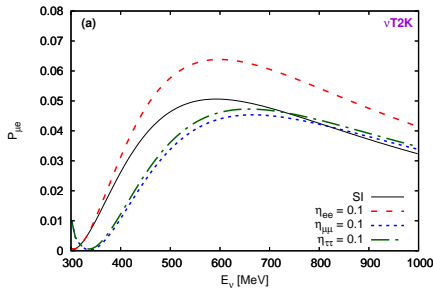
$$P_{ee}^{\text{sun}} = \left| U_{ei}^{\text{prod}} (U_{ei}^{\text{vac}})^* \right|^2$$



# Fitting the Borexino 2017 Data



# Scalar NSI @ Accelerator Neutrino Oscillation



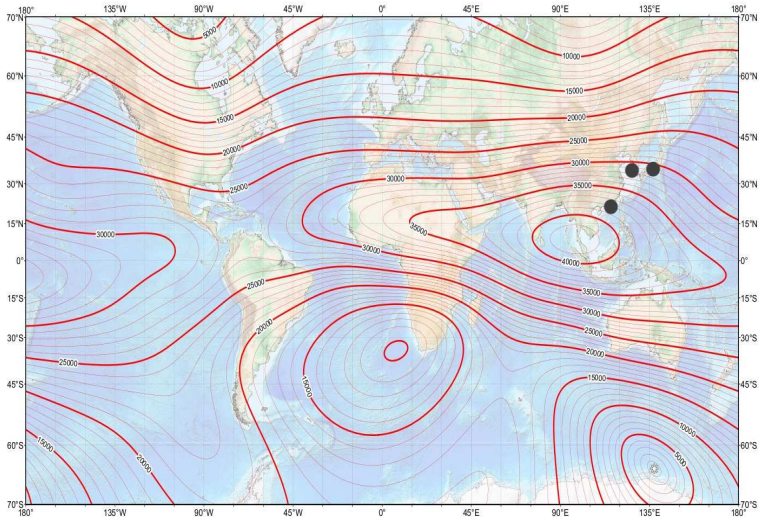
- **Better CP measurement than T2K**
  - Much larger event numbers
  - Much better CP sensitivity around maximal CP
  - Solve degeneracy between  $\delta_D$  &  $\pi - \delta_D$
  - Guarantee CP sensitivity against NUM
  - Guarantee CP sensitivity against NSI (vector & scalar)
- **Better configuration than DAE $\delta$ ALUS**
  - Only one cyclotron
  - 100% duty factor
  - Much lower flux intensity
  - Much easier
  - Much cheaper
  - Single near detector

**Thank You!**



# Lowest Atmospheric Neutrino Background

US/UK World Magnetic Model -- Epoch 2010.0  
Main Field Horizontal Intensity (H)



# Backgrounds to IBD ( $\bar{\nu}_e + p \rightarrow e^+ + n$ )

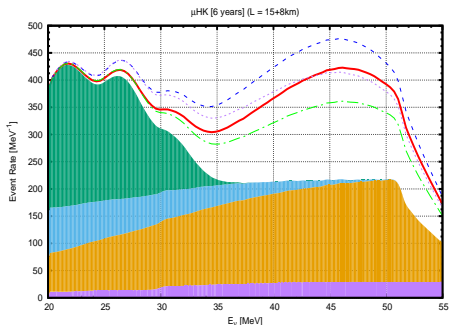
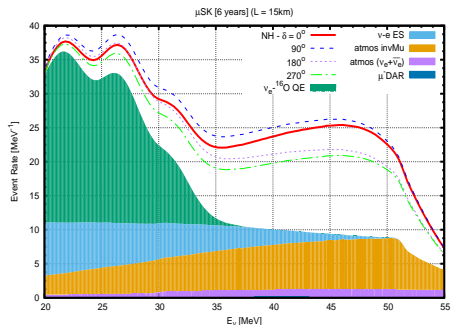
- Reactor  $\bar{\nu}_e$ :  $E_\nu < 10$  MeV
- Accelerator  $\nu_e$ :  $E_\nu > 100$  MeV
- Spallation:  $E_\nu \lesssim 20$  MeV
- Supernova Relic Neutrino:  $E_\nu \lesssim 20$  MeV

Cut with  $30 \text{ MeV} < E_\nu < 55 \text{ MeV}$

- Accelerator  $\nu_\mu \rightarrow$  **Invisible muon**
- Atmospheric Neutrino Background
  - **Invisible muon** (below Cherenkov limit)
    - $E_\mu \lesssim 1.5 \times m_\mu$ ,  $\mu^\pm \rightarrow e^\pm$
    - $E_\pi \lesssim 1.5 \times m_\pi$ ,  $\pi^+ \rightarrow \mu^+ \rightarrow e^+$
    - 1 neutron
    - No prompt photon
  - Irreducible  $\bar{\nu}_e$ :  $30 \text{ MeV} \lesssim E_\nu \lesssim 55 \text{ MeV}$
  - Reducible  $\nu_e$ :  $60 \text{ MeV} \lesssim E_\nu \lesssim 100 \text{ MeV}$ 
    - 1 neutron
    - No prompt photon
  - **Lowest** at  $\mu$ DARTS & TNT2K sites

# Event Shape @ TNT2K

Evslin, Ge & Hagiwara [1506.05023]



Expected  $\mu\text{DAR}$  IBD signal from 6 yrs of running @ SK (15km) & HK (23km) with NH.

Simulated by NuPro, <http://nupro.hepforge.org/>

# Mass Scale & Unphysical CP Phases in Oscillation

- The **effective mass term** is a combination

$$MM^\dagger \rightarrow (M + M_S)(M + M_S)^\dagger = MM^\dagger + MM_S^\dagger + M_S M^\dagger + M_S M_S^\dagger$$

- The **absolute neutrino mass** can enter neutrino oscillation!

$$MM_S^\dagger + M_S M^\dagger$$

- The **unphysical CP phases** can also enter neutrino oscillation!

$$M \equiv R_\nu D_\nu R_\nu^\dagger \quad \& \quad R_\nu \equiv P_\nu U_\nu Q_\nu$$

The **Majorana rephasing matrix**  $Q_\nu = \{e^{i\delta_{M1}/2}, 1, e^{i\delta_{M3}/2}\}$  can be absorbed,  $Q_\nu D_\nu Q_\nu^\dagger = D_\nu$  while the **unphysical rephasing matrix**  $P_\nu \equiv \{e^{i\alpha}, e^{i\beta}, e^{i\gamma}\}$  can not be simply rotated away now:

$$M \rightarrow \tilde{M} = U_\nu D_\nu U_\nu^\dagger, \quad M_S \rightarrow \tilde{M}_S = P_\nu^\dagger M_S P_\nu$$

# Parametrization & Constant Density Subtraction

- Use **characteristic scale**  $\Delta m_a^2$  to parametrize scalar NSI

$$\tilde{\mathbf{M}}_S \equiv \sqrt{\Delta m_a^2} \begin{pmatrix} \eta_{ee} & \eta_{\mu e}^* & \eta_{\tau e}^* \\ \eta_{\mu e} & \eta_{\mu\mu} & \eta_{\tau\mu}^* \\ \eta_{\tau e} & \eta_{\tau\mu} & \eta_{\tau\tau} \end{pmatrix},$$

where  $\Delta m_a^2 \equiv \Delta m_{31}^2 = 2.7 \times 10^{-3} \text{ eV}^2$ .

- We first need **input** for  $\tilde{\mathbf{M}}$  which is not directly measured.
- However, the directly measured from terrestrial experiments is always a combination,  $\tilde{\mathbf{M}} + \tilde{\mathbf{M}}_S (\rho_s \approx 3\text{g/cm}^3)$ . It is then necessary to first subtract a constant term:

$$\tilde{M} \rightarrow \tilde{M} + \tilde{\mathbf{M}}_S \frac{\rho - \rho_s}{\rho_s}$$

where  $\tilde{\mathbf{M}} = \mathbf{U}_\nu \mathbf{D}_\nu \mathbf{U}_\nu^\dagger$  is **reconstructed** in terms of the measured mixing matrix while  $\tilde{M}_S$  is the scalar NSI @ typical constant **subtraction density**  $\rho_s$ .

# Scalar NSI @ Atmospheric Neutrino Oscillation

